



Brokering of Theorem Proving Services Described in MSDL

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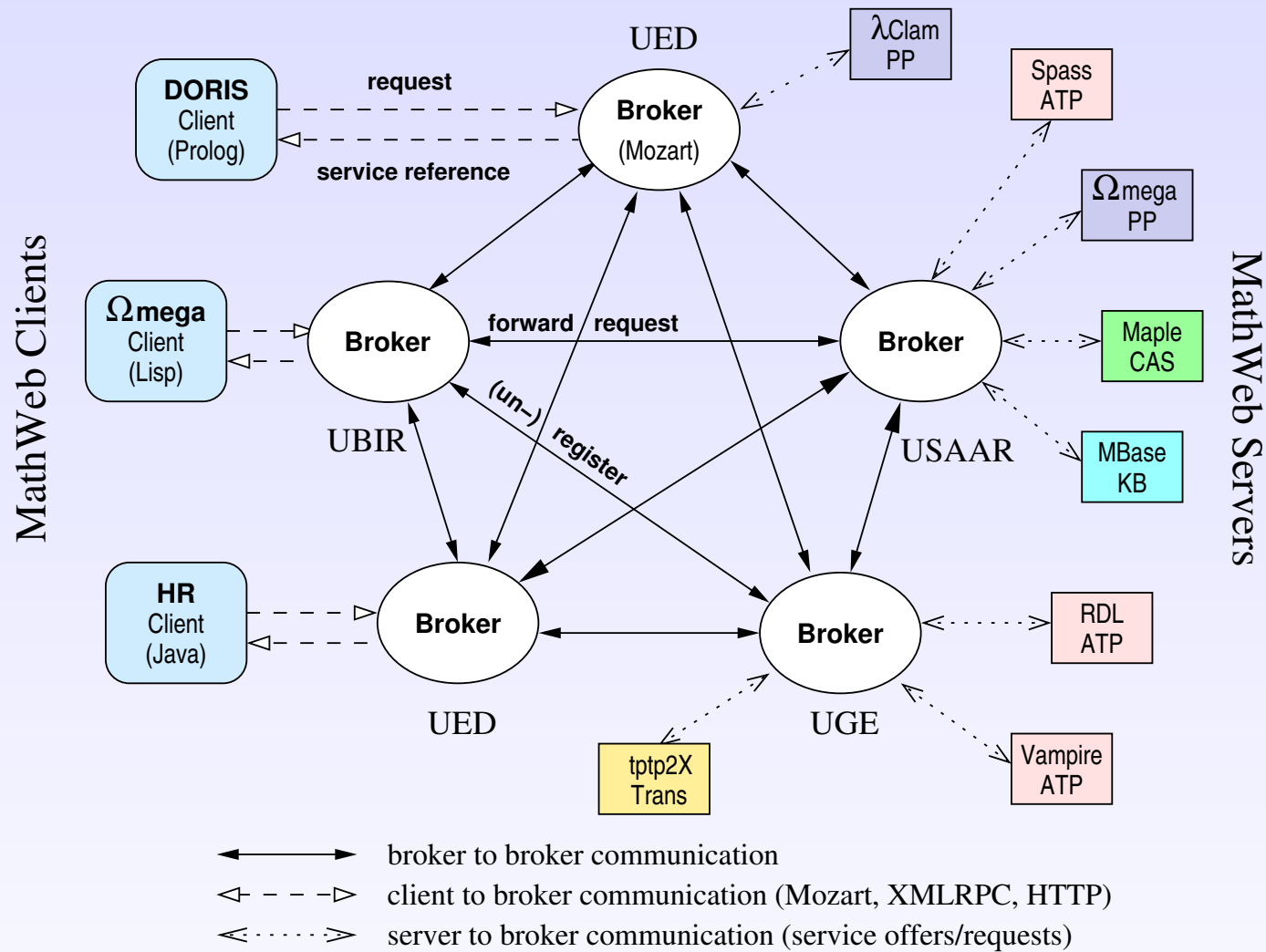
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Overview

- Motivation
- Our Agent Framework
- An Ontology for Deductive Services
- First-order ATP Services
- Classification of Theorem Proving Problems
- Broker for FO-ATP Services
- A Little Demonstration

Motivation



Motivation

Despite its success, MathWeb-SB some limitations:

- Client applications still have to know
 - **which reasoning system** to use, and
 - **how to access** the system.
- User has to **coordinate different reasoning systems** to solve a problem.
- The MathWeb-SB is not designed for asynchronous communication.
- Technical Problems (OS, Firewalls, Proxies)

A New Agent Framework

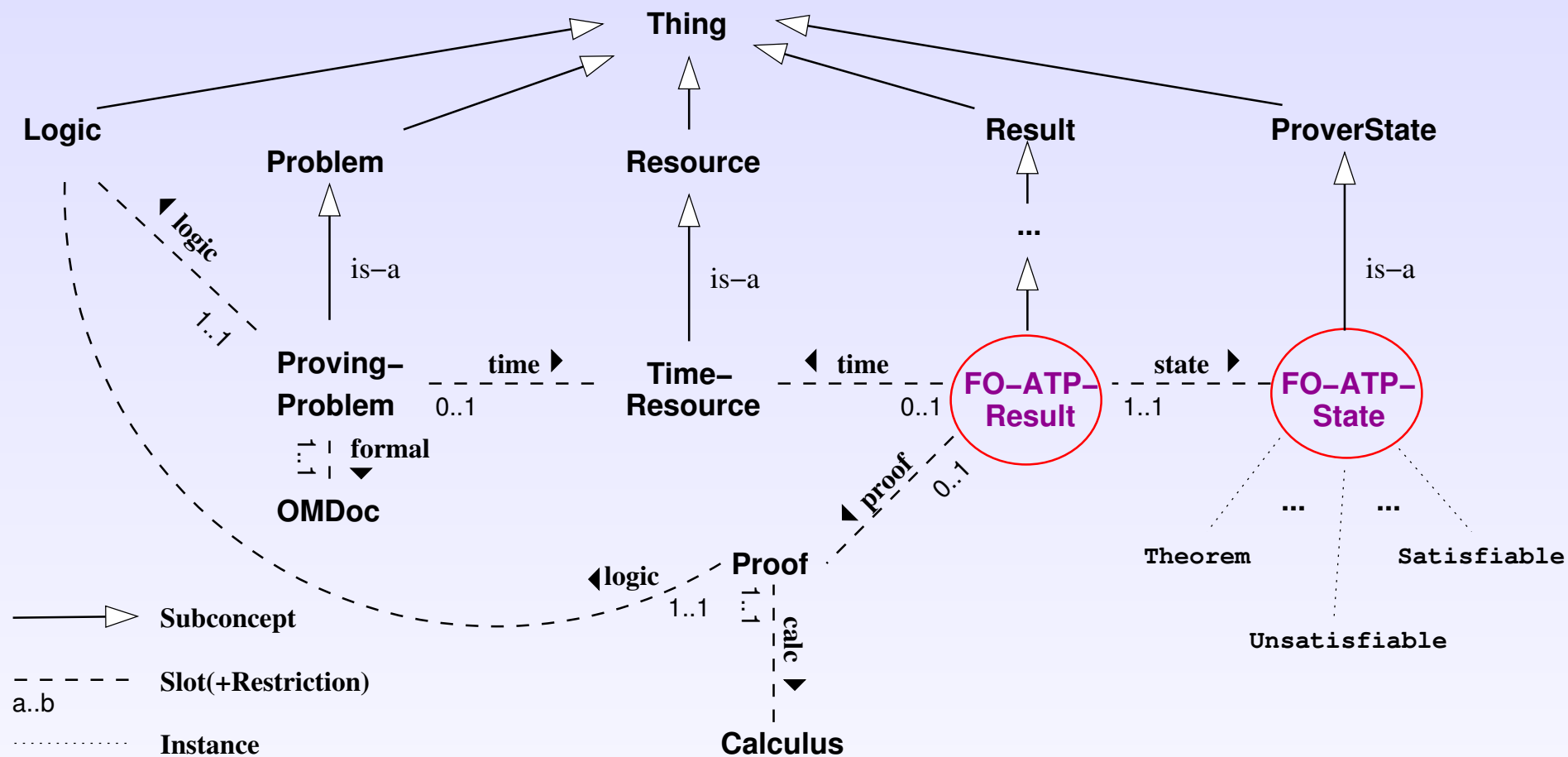
From MathWeb-SB to the Semantic MathWeb-SB:

- ... based on **FIPA compliant agent** platform (**JADE**)
- ... agents offering reasoning **services described in service description language**:
 - ⇒ currently **MSDL**
(developed in MONET and MathBroker)
 - ⇒ in the future also **OWL-S (OWL)**?
- ... a **brokering mechanism** for reasoning services.

Ongoing Work

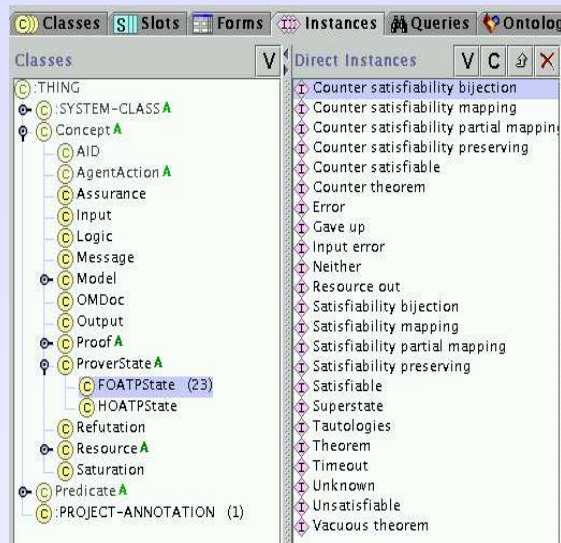
- Implementing **agents and communication** in JADE
- Designing an **Ontology** in **Protégé-2000** tool (Protégé-2 supports OWL).
- Describing **first-order Automated Theorem Provers** (ATPs) in MSDL using our ontology.
- Mapping **MSDL** to Java classes.
- Implementing simple **brokering**:
 - analysing problems in queries.
 - find most suitable service.

An Ontology for Deduction Services



One Ontology for All

Protege Ontology:



JADE Agent Ontology:

```
package org.mathweb.onto;
import jade.content.*;
import jade.util.leap.*;
import jade.core.*;

public class FOATPState extends ProverState{
private List returns = new ArrayList();
public void addReturns(Assurance o) {returns.add(o);}
public boolean removeReturns(Assurance o) {return returns.remove(o)}
public void clearAllReturns() {returns.clear();}
...
}
```

Beangenerator

JiBX?

Ontology for Services (MSDL):

```
...
<input name='problem'>
  <signature>
    http://www.mathweb.org/ontology/atp#TPTPProblem
  </signature>
</input>
...
```


First-order Theorem Proving Services

Every first-order **proving service**...

- ... accepts standard problem formats **TSTP** and **OMDoc**.
- ... returns a **proof object** in standard format (**TSTP**).
- ... is **specialized** on a particular domain.

For an **ontology** for first-order ATPs use:

- Experience with the MathWeb-SB.
- Recent work with Geoff Sutcliffe and Stephan Schulz on **ATP states**.

First-order Theorem Proving Problems

FO proving problems classified using known features
(Sutcliffe & Suttner 2001):

- Logical Class of problem:
 - *essentiallyPropositional* (finite Herbrand Universe)
 - *realFirstOrder*
- Equality: *noEquality*, *someEquality*, *pureEquality*
- Presentation: *fofForm* (first-order formulae)
vs. *cnfForm* (clause normal form)

⇒ 16 “Specialists Problems Classes” (SPC)

Performance data of well-known ATPs is available for every SPC.

The ATP SPASS in MSDL

Service: SpassProver	
classification:	Classification with Taxonomy of services or link to Ontology (\rightarrow QPQ) ● \rightarrow spass problem description
service interface:	(\rightarrow fo-prover.wsd1)
implementation details:	Information about hardware, software (calculus, etc.)

spass problem description	
input parameters:	name: <i>problem</i> , signature: FO-ATP-Problem (Ontology concept)
output parameters:	name: <i>result</i> , signature: FO-ATP-Result (Ontology concept)
pre-conditions:	<i>essentiallyPropositional</i> (<i>problem</i>) (OpenMath Object) \wedge <i>noEquality</i> (<i>problem</i>) \wedge <i>f of Form</i> (<i>problem</i>)
post-conditions:	

The ATP E in MSDL

Service: EProver	
classification:	Classification with Taxonomy of services or link to Ontology (\rightarrow QPQ) ● \rightarrow e problem description
service interface:	(\rightarrow fo-prover.wsd1)
implementation details:	Information about hardware, software (calculus, etc.)

e problem description	
input parameters:	name: <i>problem</i> , signature: FO-ATP-Problem (Ontology concept)
output parameters:	name: <i>result</i> , signature: FO-ATP-Result (Ontology concept)
pre-conditions:	$realFirstOrder(problem)$ $\wedge pureEquality(problem)$ $\wedge nonUnitPureEquality(problem)$
post-conditions:	

A First Broker

Our broker ...

- ... **analyses** incoming proving problems using **TSTP classifier** (G. Sutcliffe).
- ... **annotates** problems with new preconditions \Rightarrow puts problem in **SPC**.
- ... **matches** new problem with available services using **tuProlog** engine (DEIS, Università di Bologna).
- ... **calls** the first matching service.

A little Demo

- Two services: EProver & SpassProver

- Two queries:

- **Query 1:** Did Agatha commit suicide?

$\forall x. \text{Agatha hates } x \Rightarrow \text{Butler hates } x, \dots$

classified as *essentiallyPropositional*, *noEquality*, *f of F form*

- **Query 1:** Problem in group theory:

$\forall x. x * e = x \wedge \forall x. x * x^{-1} = e \wedge \forall x. x * x = e \wedge \forall x. a * b = c$

$\vdash b * a = c$

classified as *realFirstOrder*, *pureEquality*, *nonUnitPureEquality*

- Consequently, broker selects
SpassProver for **Query 1** and
EProver for **Query 2**.

Problems To Solve

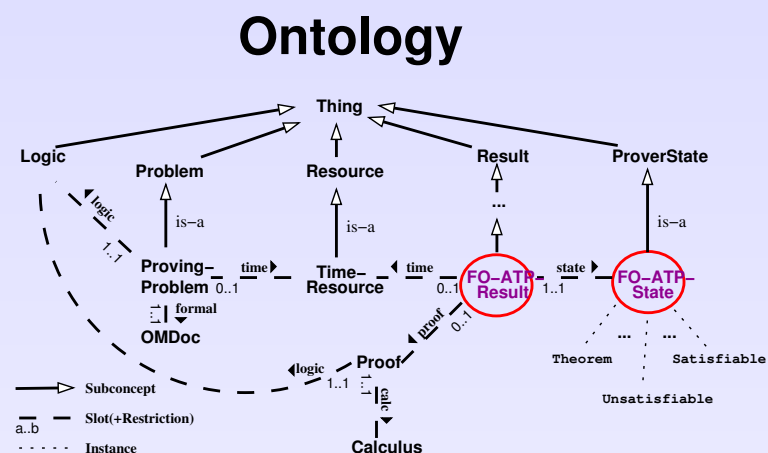
Among others...

- **Binding** of MSDL to agent Ontology
Currently, we use **JiBX**. Mathbroker uses JAXB.
- **I/O parameters** of MSDL abstract problems:
⟨OMOBJ⟩ vs. XML-serialisation of Java Objects
(FO-ATP-Problem)
- Invocation of service through JADE **agent behaviours**
(conversations).
- **Combination of behaviours**.

Future Work

- **Knowledge retrieval** from ATP users and developers.
- **Case study** to show benefit of brokering.
- Extend ontology to logics & calculi.
- **SOAP binding** for MONET and Mathbroker.
- Ontology in OWL (\rightarrow Protege-2.0 & HarmonIA).
- **Description of other reasoning systems**
(e.g., model generators).
- Advanced brokering (dynamic combination of services).

A Dream: MSDL Service Authoring Tool



Repository of already specified JADE Agent Behaviours

```

<DialogicFramework id="FishDialFrw" contentLanguage="en">
  <Ontology id="FishONTO" specificationLanguage="MSDL">
    <Role id="Boss" type="InternalRole">
      <Behaviour id="Open" type="SimpleBehaviour"/>
      <Behaviour id="Discuss" type="CompositeBehaviour">
        <Behaviour id="InitialResolution" type="OneShotBehaviour"/>
        <Behaviour id="FinalResolution" type="OneShotBehaviour"/>
      </Behaviour>
    </Role>
  </Ontology>
</DialogicFramework>
  
```

